# Oceanographic modeling and data assimilation: Adapting tools to support MRV for CDR

## **Matthew Long**

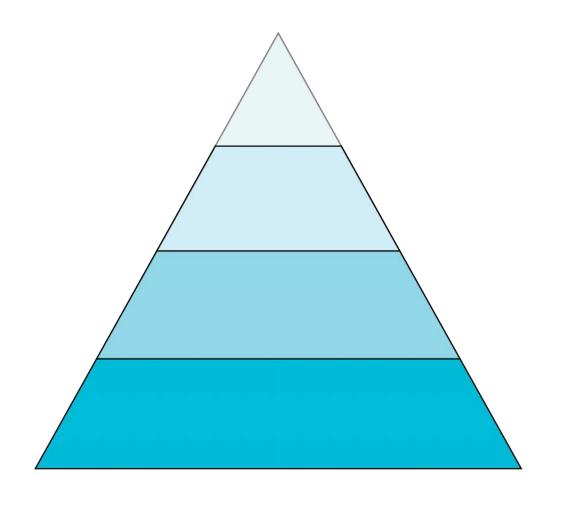
Climate & Global Dynamics Laboratory
National Center for Atmospheric Research



NSF

16 June 2022

## Modeling frameworks to support ocean CDR & MRV



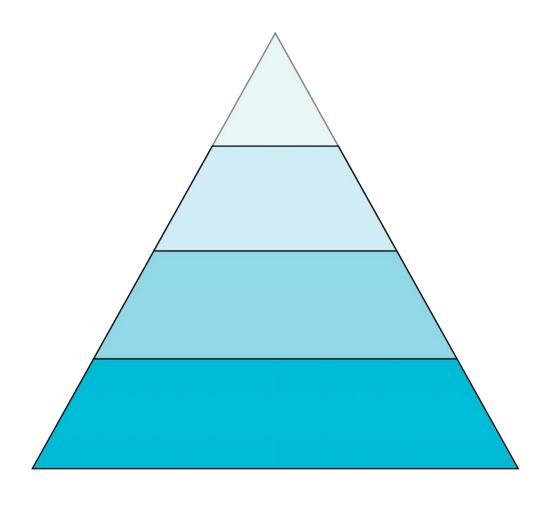
CDR processes & experimental framework

Observing system design Verification with sequential data assimilation

Data assimilation

Ocean physical and biogeochemical models

## Modeling frameworks to support ocean CDR & MRV



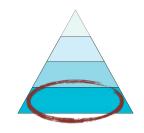
CDR processes & experimental framework

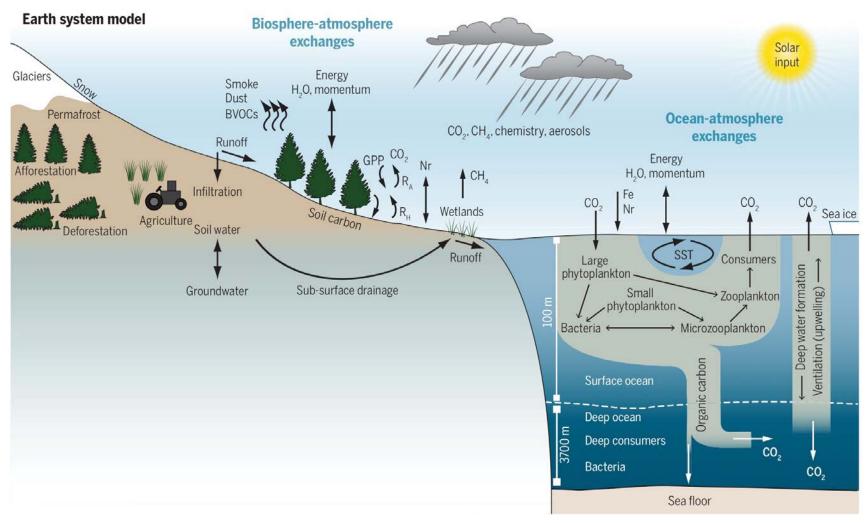
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Ocean physical and biogeochemical models

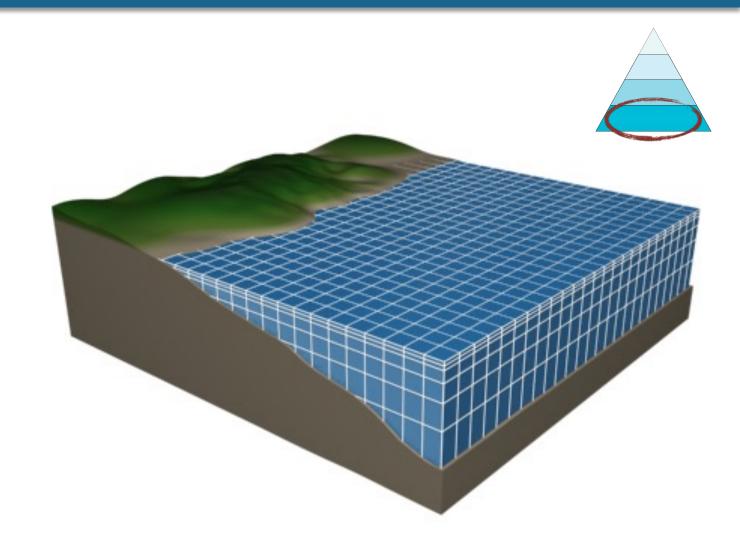
## **Earth system models**

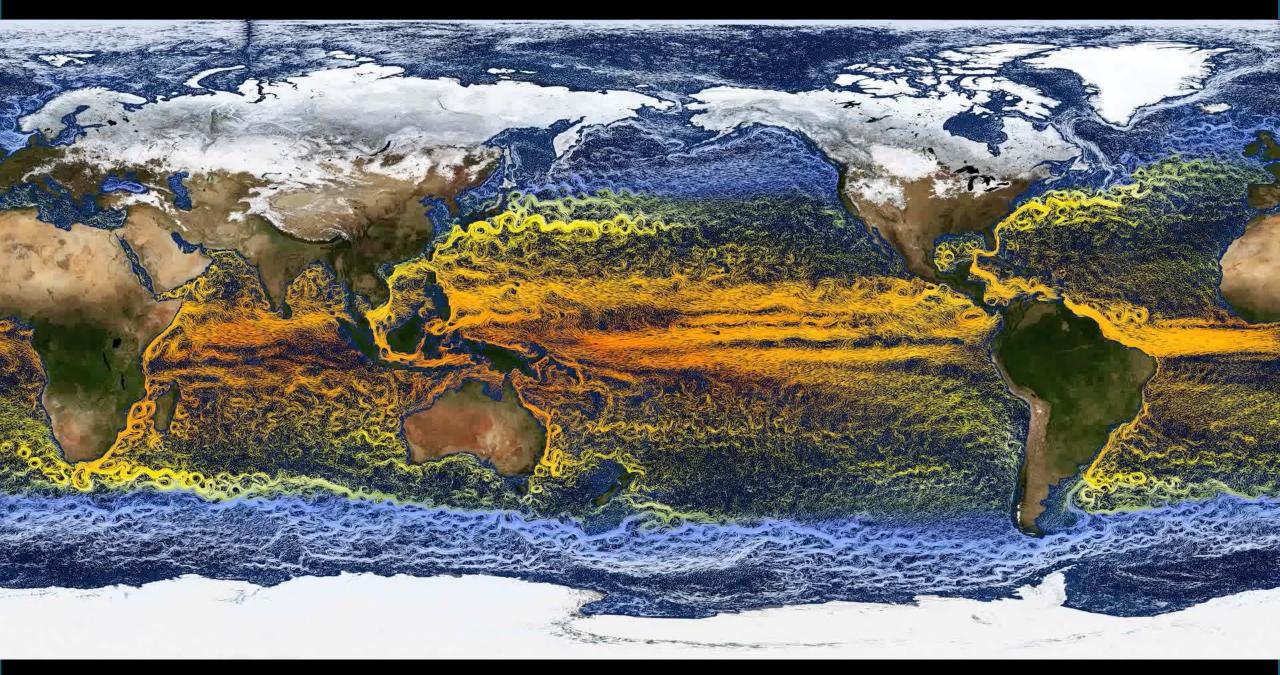




Navier-Stokes: Equations are "exact", but cannot be solve analytically

General Circulation Models (GCMs) implement numerical solutions on discrete grid



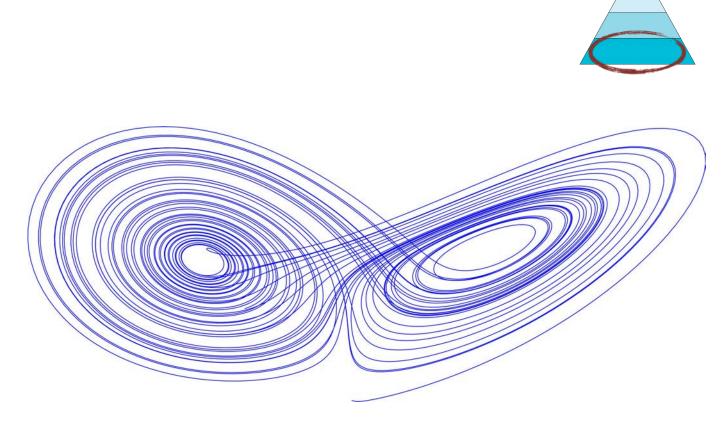


Navier-Stokes: Equations are "exact", but cannot be solve analytically

General Circulation Models (GCMs) implement numerical solutions on discrete grid

Deterministic, but chaotic:

- Perpetual novelty
- Infinite sensitivity to initial conditions

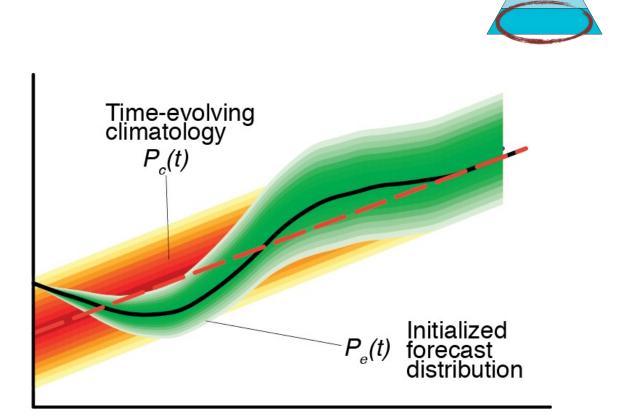


Navier-Stokes: Equations are "exact", but cannot be solve analytically

General Circulation Models (GCMs) implement numerical solutions on discrete grid

Deterministic, but chaotic:

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Time

Navier-Stokes: Equations are "exact", but cannot be solve analytically

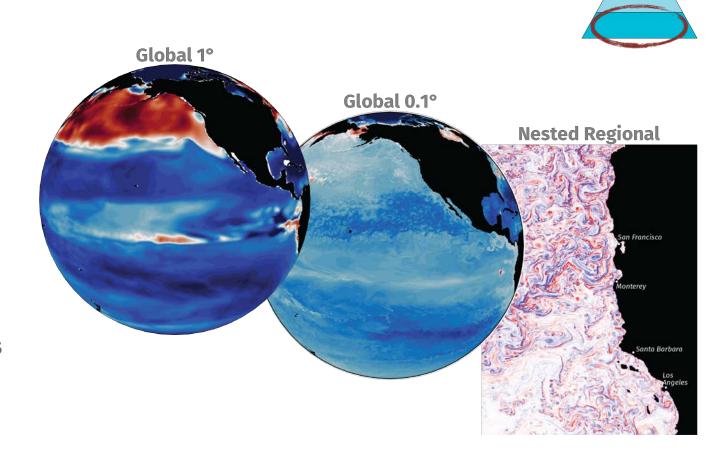
## Primitive equation models:

- Numerical solutions on discrete grid
- General Circulation Models (GCMs)

## Deterministic, but chaotic:

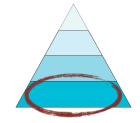
- Perpetual novelty
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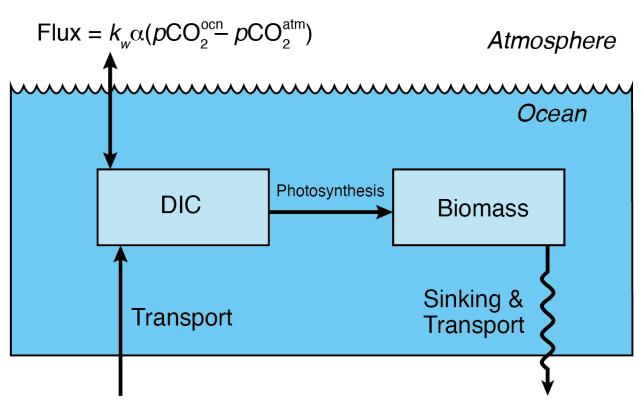
Scale interactions: energy cascade requires parameterization of subgrid-scale effects





Biology sets upper ocean DIC budget





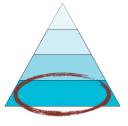
Dissolved inorganic carbon 
$$DIC = \begin{bmatrix} \mathsf{H}_2\mathsf{CO}_3^* \end{bmatrix} + \begin{bmatrix} \mathsf{HCO}_3^- \end{bmatrix} + \begin{bmatrix} \mathsf{CO}_3^{2-} \end{bmatrix} \\ \sim 0.5\% \qquad \sim 88.6\% \qquad \sim 10.9\%$$

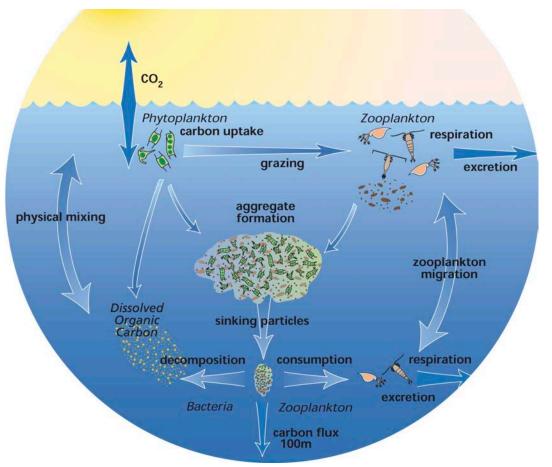
Biology sets upper ocean DIC budget

Ecosystem function controls **C** export

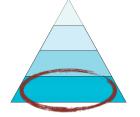
There are no universally-accepted governing equations:

- Plankton function types
- Transfer functions





Biology sets upper ocean DIC budget

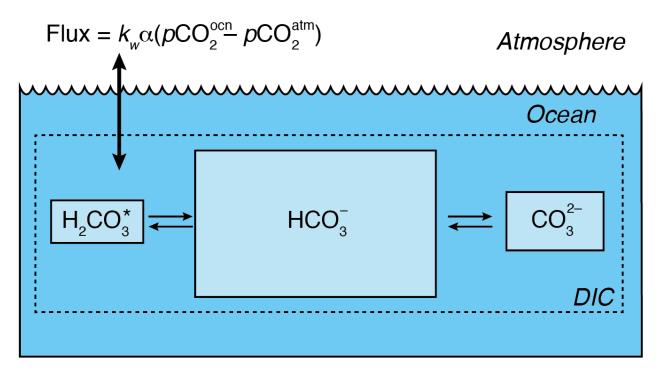


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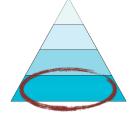
- Plankton function types
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Explicit carbon chemistry



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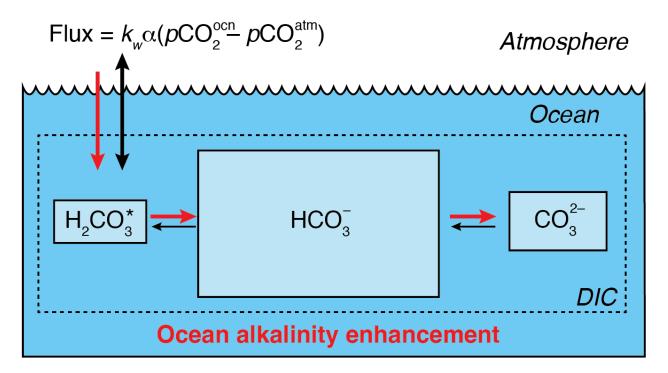


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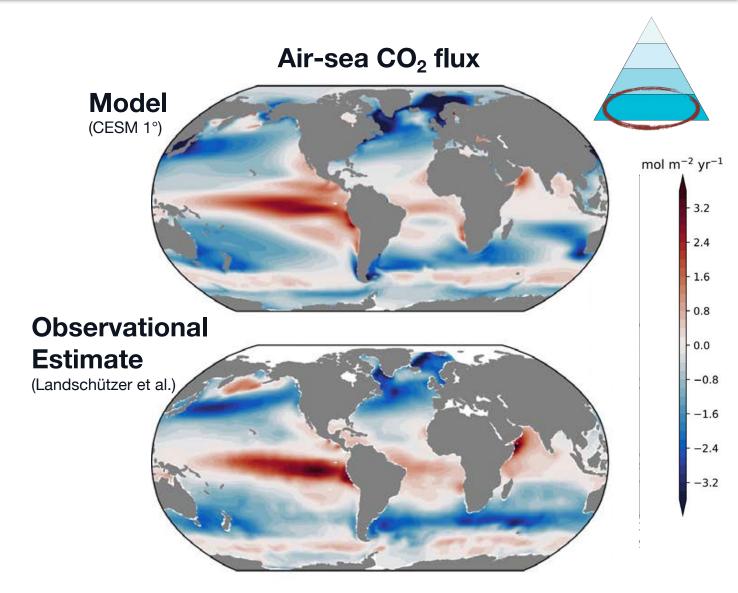
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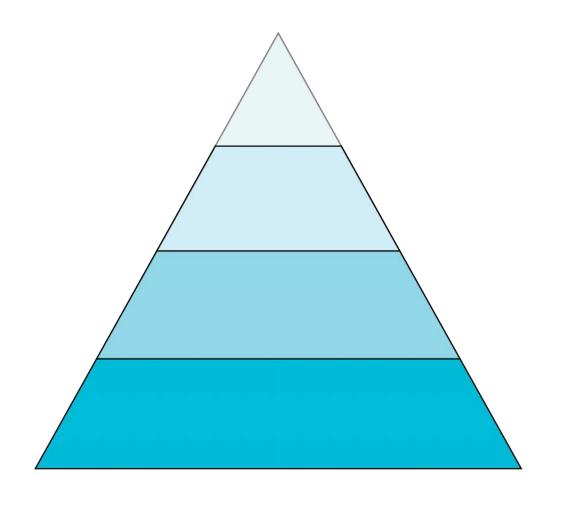
- Plankton function types
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Explicit carbon chemistry

Models are built at the process-level; simulations show emergent features



## Modeling frameworks to support ocean CDR & MRV



CDR processes & experimental framework

Observing system design Verification with sequential data assimilation

#### **Data assimilation**

Ocean physical and biogeochemical models

#### **Data assimilation**

Free-running models display systematic bias

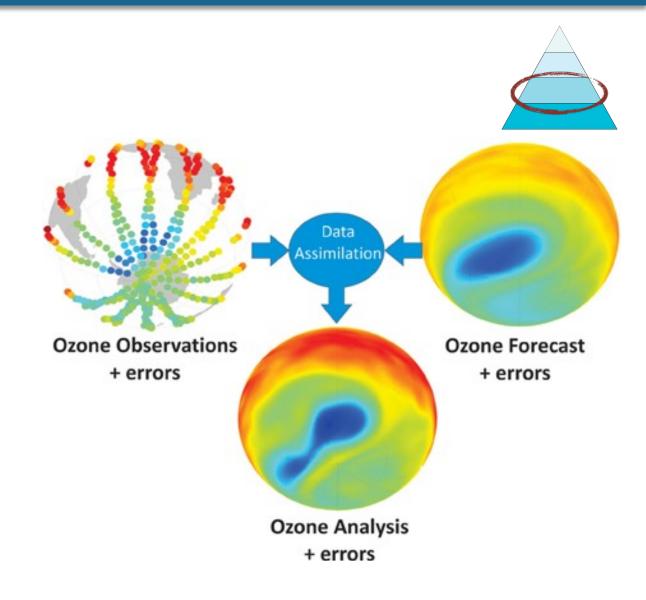
DA can produce a model-data state
estimate ("reanalysis"), reducing bias

DA provides model states that are maximally consistent with observations

DA can provide explicit uncertainty estimates and assessments of which observations are most important

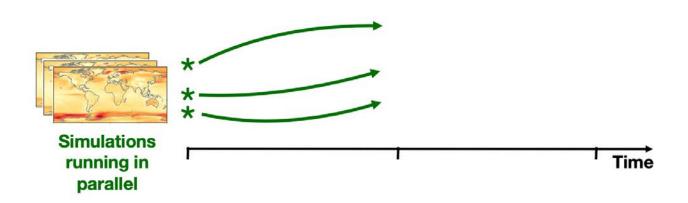
## Two approaches:

- Sequential ensemble DA (filter)
- Variational methods (smoother)



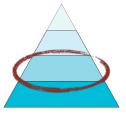
#### **Ensemble data assimilation**

Integrate ensemble of models

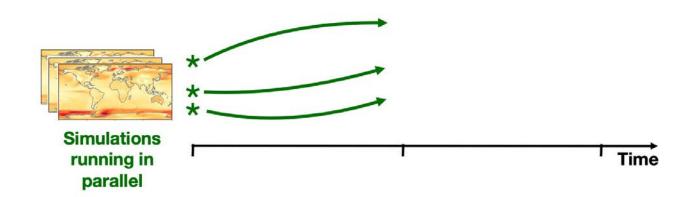


#### **Ensemble data assimilation**

Integrate ensemble of models



Observation

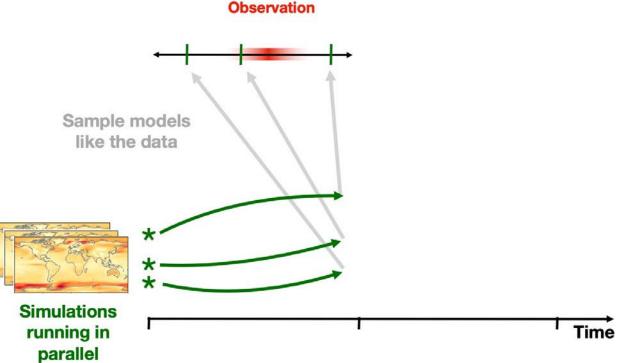


#### **Ensemble data assimilation**

Integrate ensemble of models

Sample models like the data



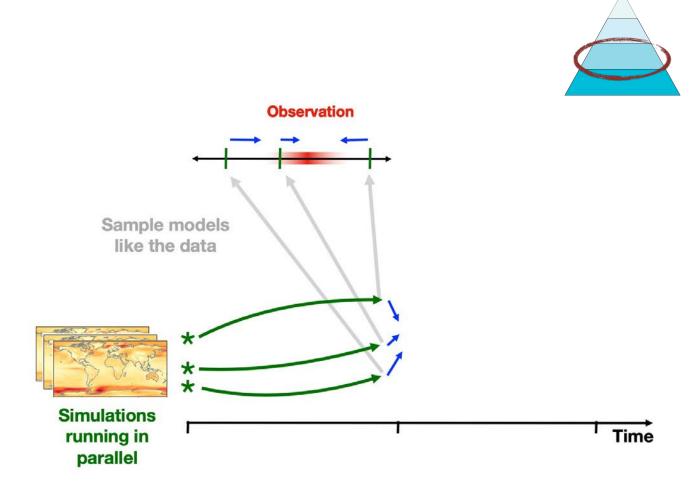


#### **Ensemble data assimilation**

Integrate ensemble of models

Sample models like the data

Add "increments" to model states to improve fit to data



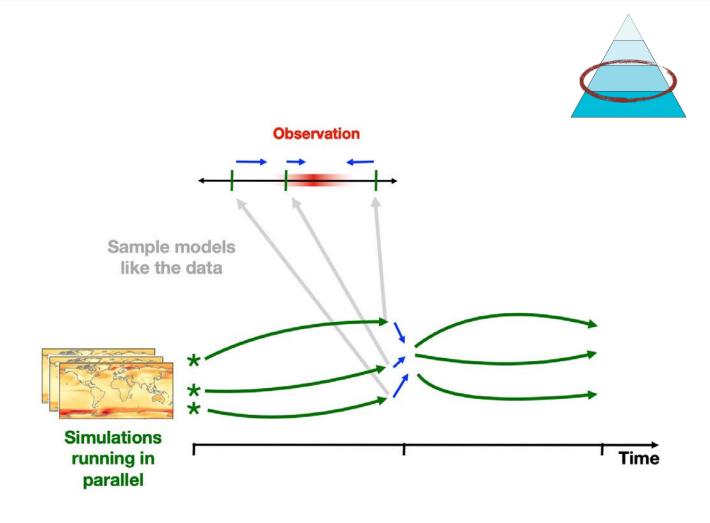
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Integrate ensemble of models

Sample models like the data

Add "increments" to model states to improve fit to data

Continue integration



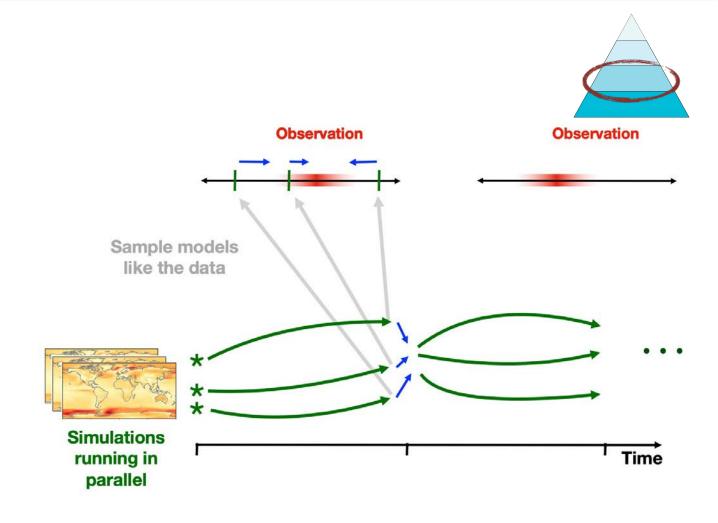
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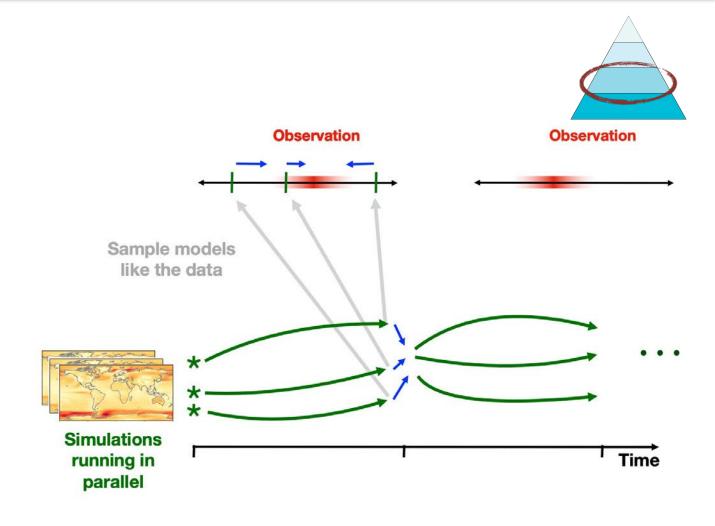
Continue integration



## **Challenges and shortcomings**

Adding increments to the state can break the model physics

Two often-necessary tools: inflation and localization



## Variational methods solve an iterative optimization problem to minimize an objective function

Example: the ECCO state estimate

Atmospheric boundary conditions

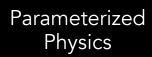
Wind stress

Radiation

Freshwater fluxes
(E-P-R)

Control variables, **u** 

Initial conditions T(0), S(0)



## Variational methods in practice: the ECCO state estimate

#### Inverse problem solved by ECCO

Solve for a set of

- initial conditions,
- atmospheric boundary forcing,
- ocean mixing parameters,

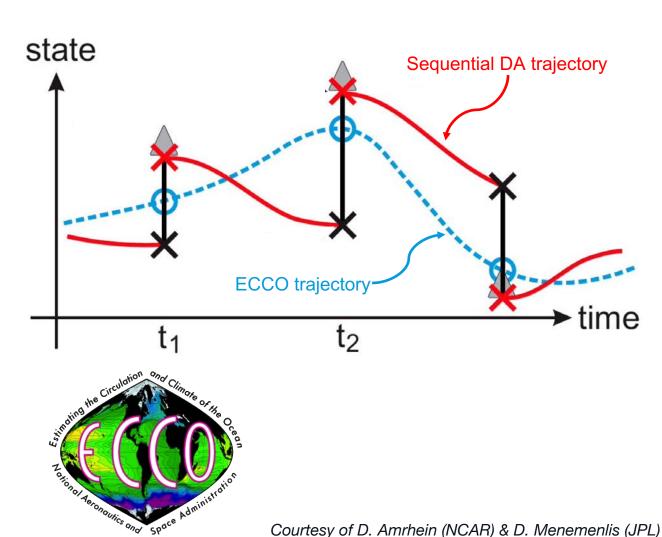
to minimize residuals between the model solution and the observations in a least-squares sense.

#### **Advantages**

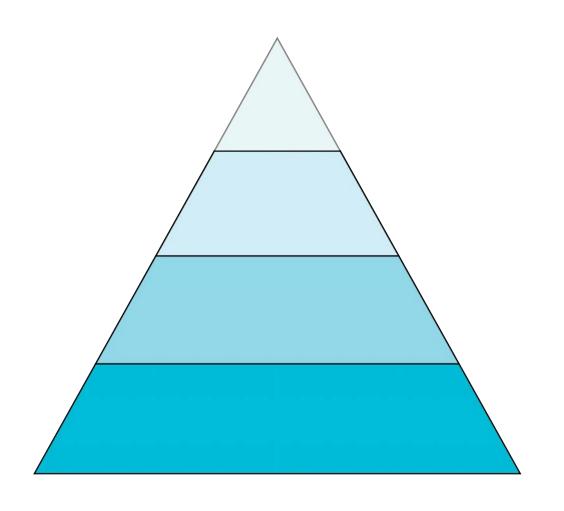
- Conserves ocean properties
- Uses information from past and future to constrain state (smoother rather than a filter)

#### **Disadvantages**

- Can generate spurious fluxes, e.g. in Lab. Sea
- No "errors of the day"
- No uncertainty quantification
- Expensive to maintain adjoint



## Modeling frameworks to support ocean CDR & MRV



CDR processes & experimental framework

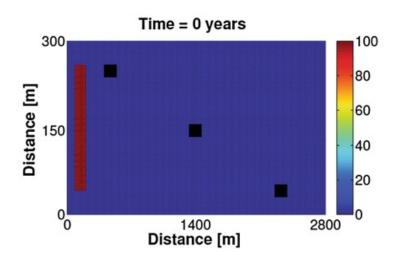
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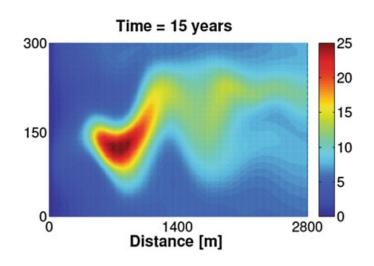
Data assimilation

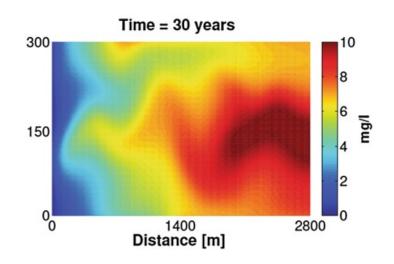
Ocean physical and biogeochemical models

## Optimization of observing location

What is an optimal sampling strategy to best constrain a quantity of interest (i.e., "verification variable")?

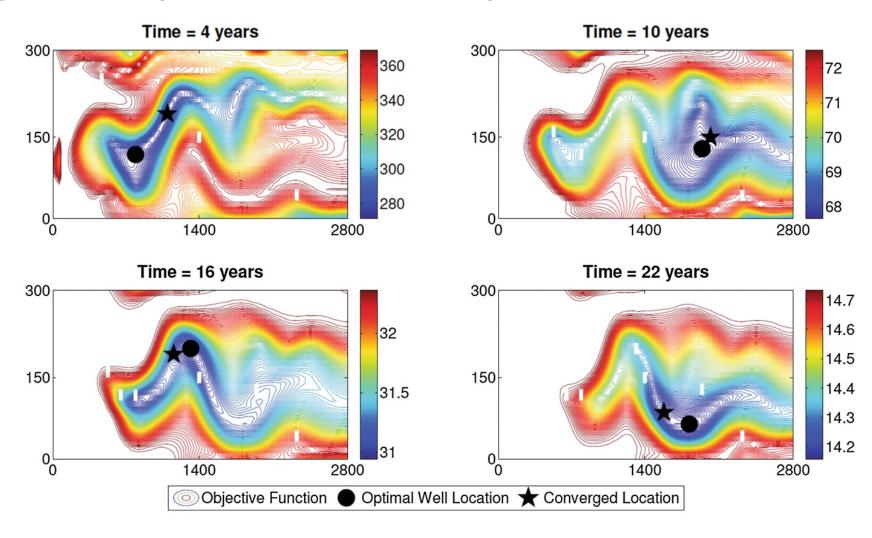






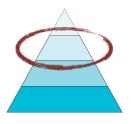
## **Optimization of observing location**

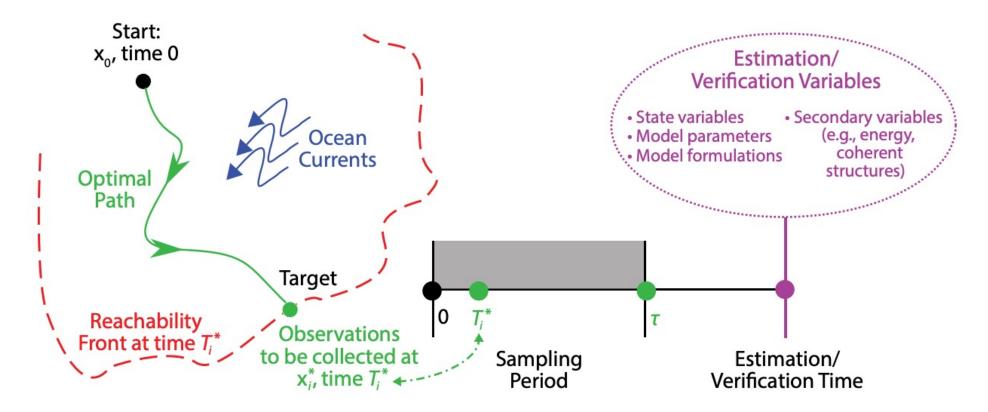
What is an optimal sampling strategy to best constrain a quantity of interest (i.e., "verification variable")?



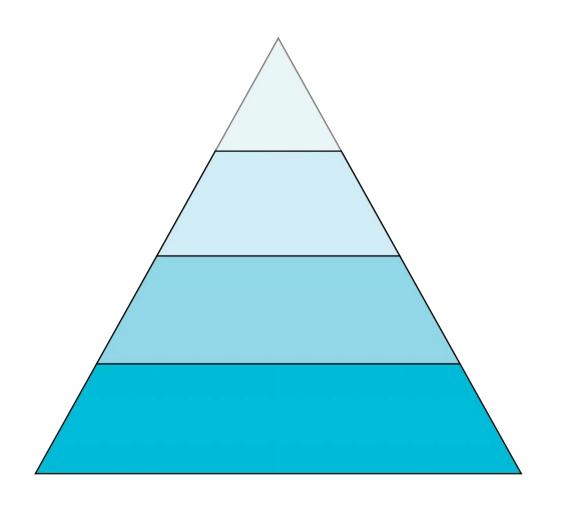
## Optimal observing system design

What is an optimal sampling strategy to best constrain a quantity of interest (i.e., "verification variable")?





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## **MRV** Challenges

Unfavorable signal-to-noise ratios

- Large background fields
- Dynamic variability

Establishing baseline counterfactual to assess additionality

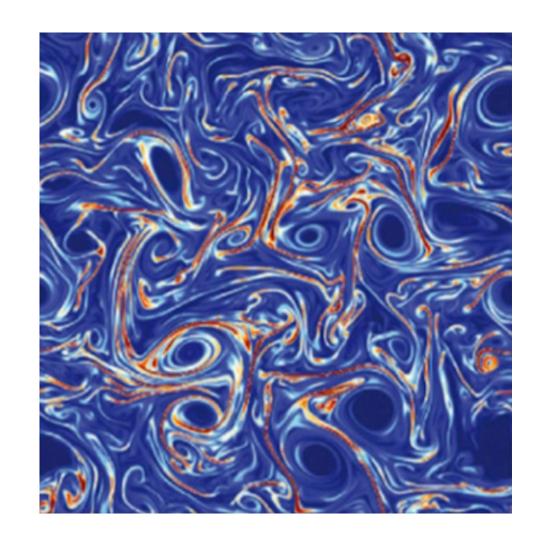
Large spatiotemporal scales

- Slow CO<sub>2</sub> equilibration timescale
- Large-scale overturning circulation

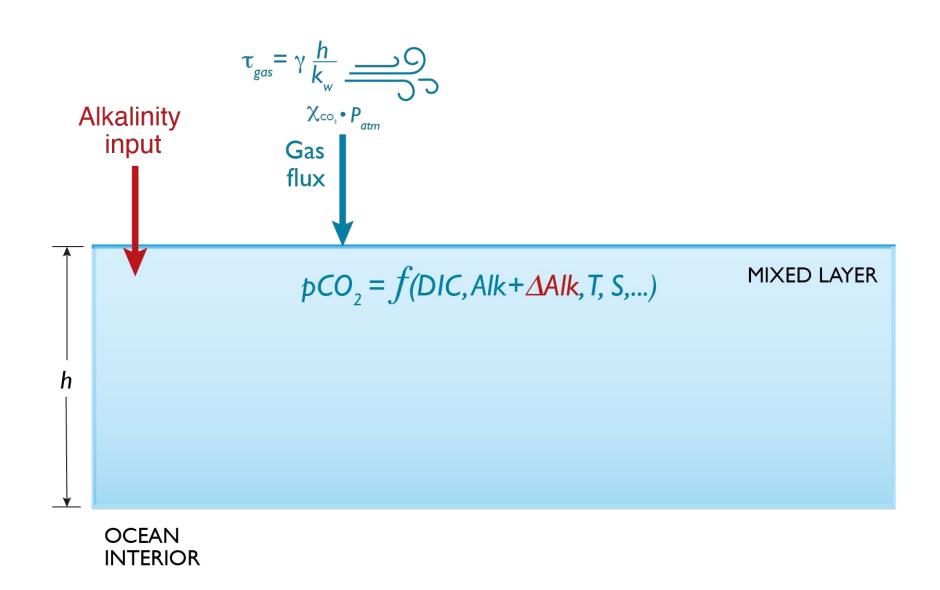
Model skill and parameter uncertainty

Unknown unknowns

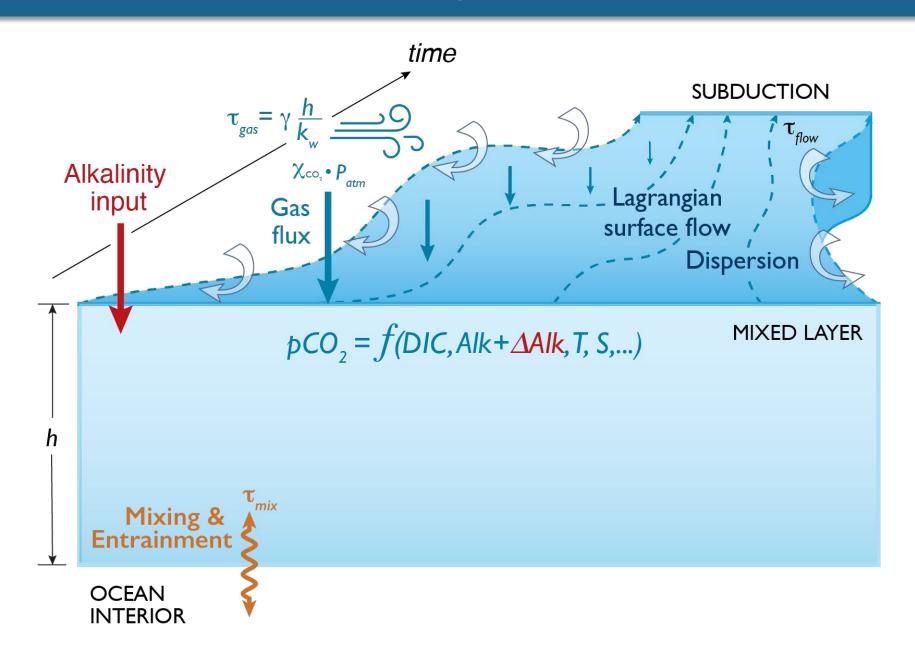
- Ecosystem compensation



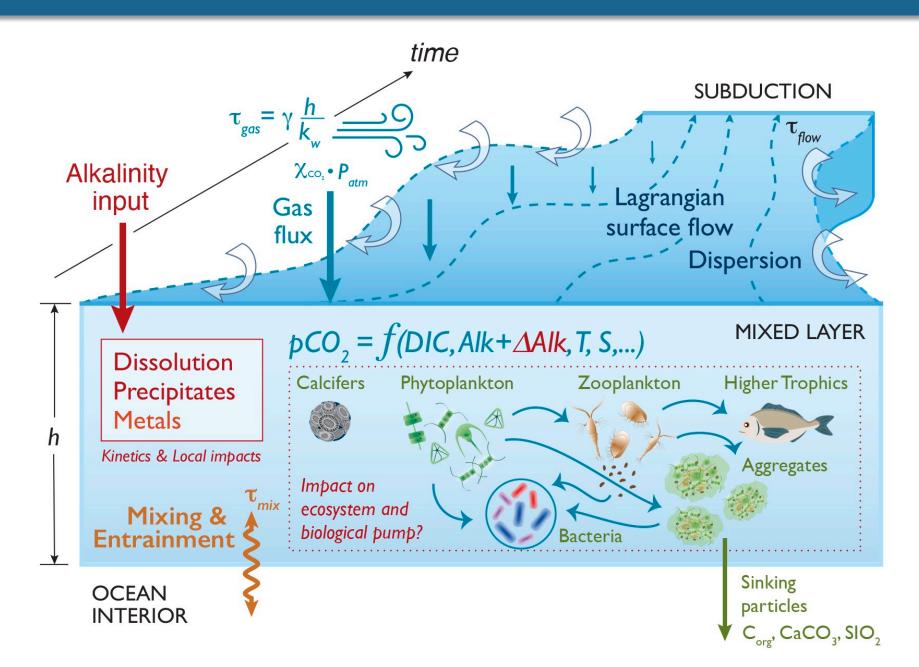
## Ocean alkalinity enhancement



## Ocean alkalinity enhancement

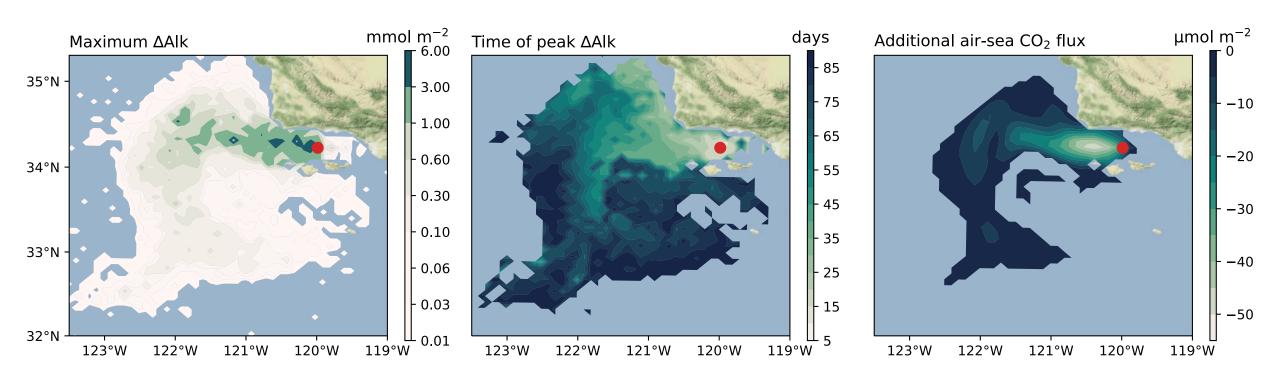


## Ocean alkalinity enhancement



## **Results from idealized experiments**

## Simulated alkalinity release (CESM 0.1°)



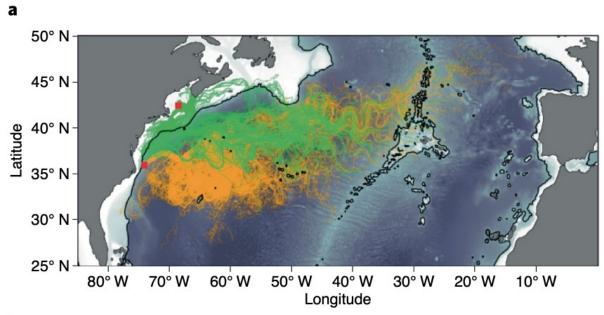
### Particle dispersion modeling

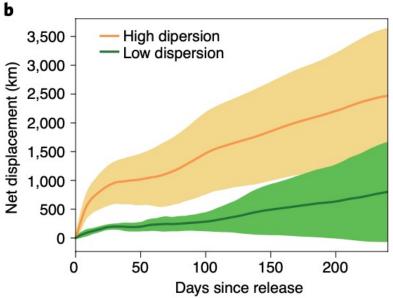
Lagrangian (i.e., flow-following) frameworks provide complementary information to GCMs

Particles can be advected in precomputed velocity fields

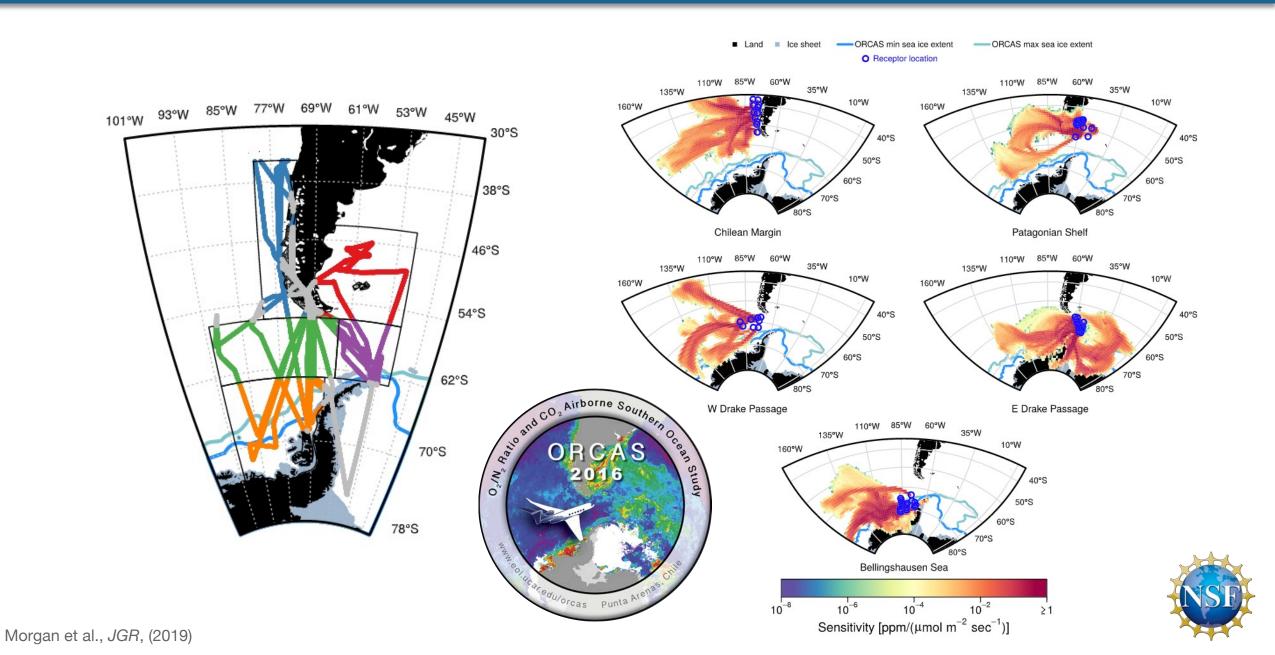
Quantify dispersion and trajectories

Possible to sample properties and compute transformations along particle paths

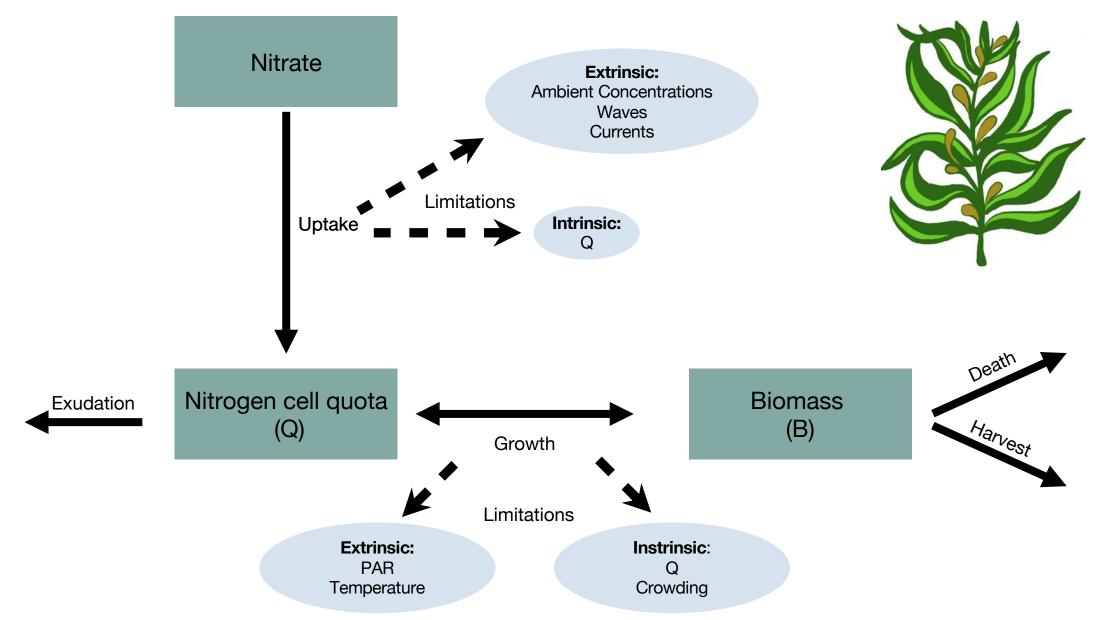




# Lagrangian back-trajectories & footprints computed for aircraft samples



# Global MacroAlgae Cultivation MODelling System (G-MACMODS)



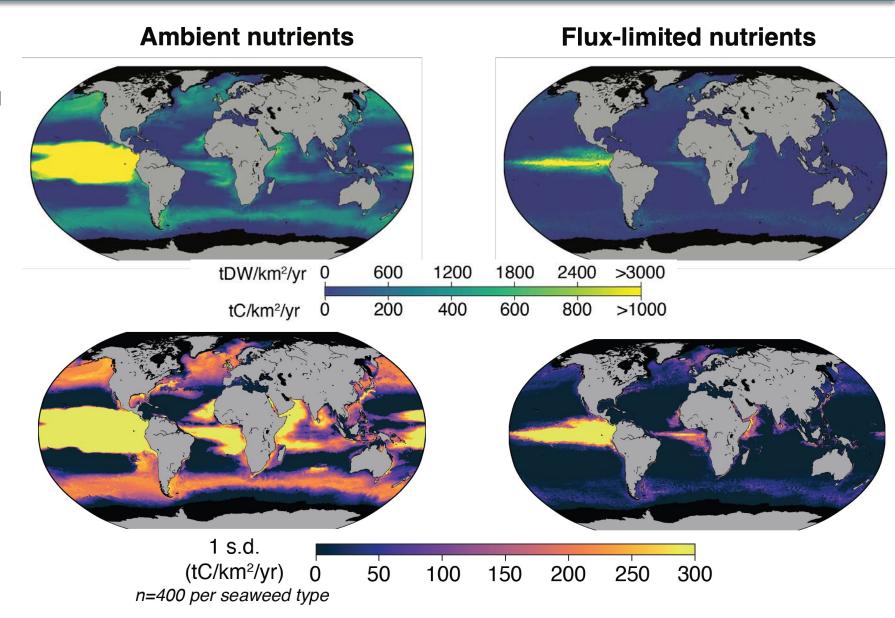
Courtesy of I. Arzeno (UCI) Frieder et al. (2022)

#### Projecting potential macroalgae yields: uncertainty in parameters

# Uncertainty analysis around biological parameters:

- Maximum uptake rate
- Half saturation constant
- Compensation irradiance
- Saturation irradiance
- Maximum growth rate
- Crowding
- · Ratio of biomass to surface area
- Minimum nitrogen cell quota
- Max nitrogen cell quota
- Drag coefficient
- Nitrogen exudation rate
- Mortality rate

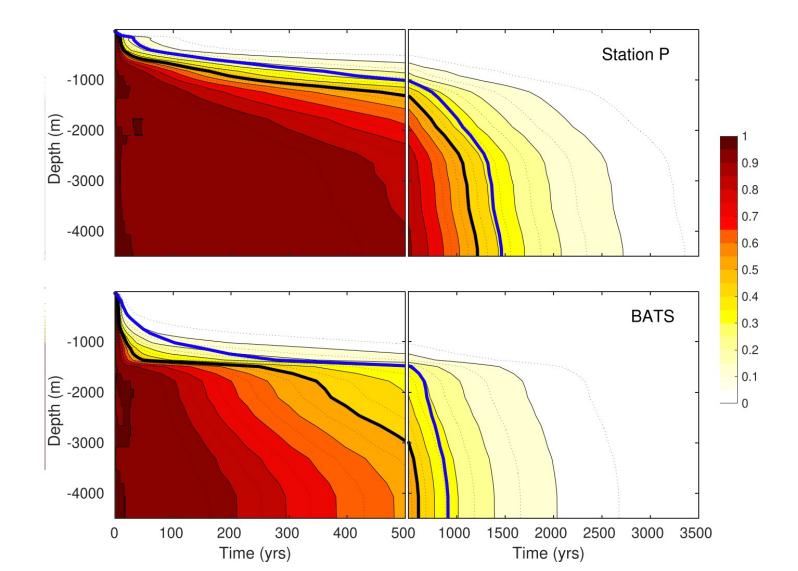
n = 400 Monte Carlo runs for each seaweed group and each nutrient scenario (ambient and flux-limited)



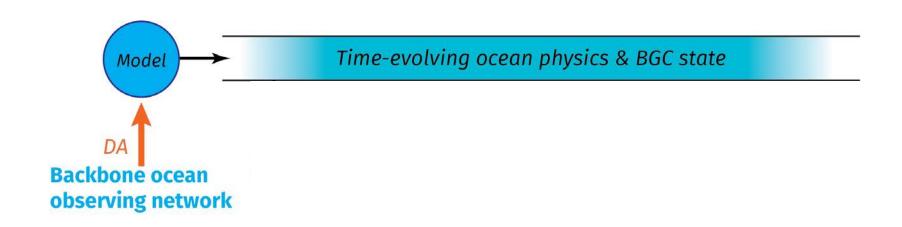
Courtesy of I. Arzeno (UCI)

# Separation of concerns: mapping re-emergence timescales

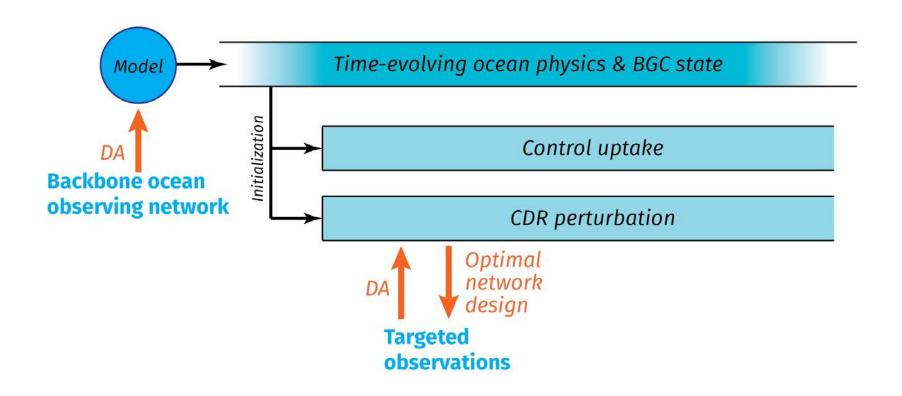
#### Fraction of carbon remaining sequestered after injection at depth



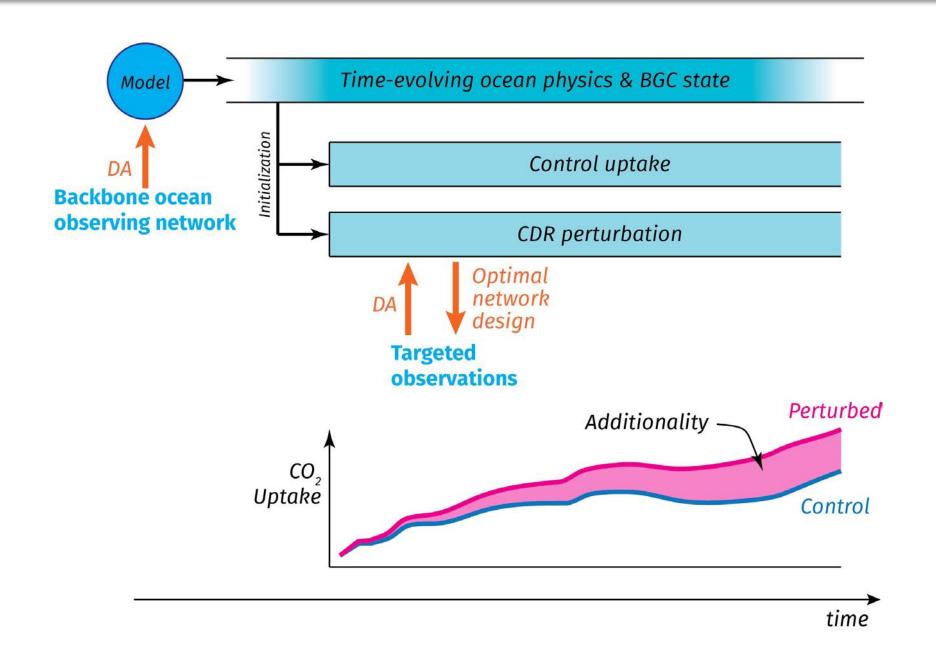
# **Experimental framework for MRV**



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# **Experimental framework for MRV**



### **Computation and data constraints**

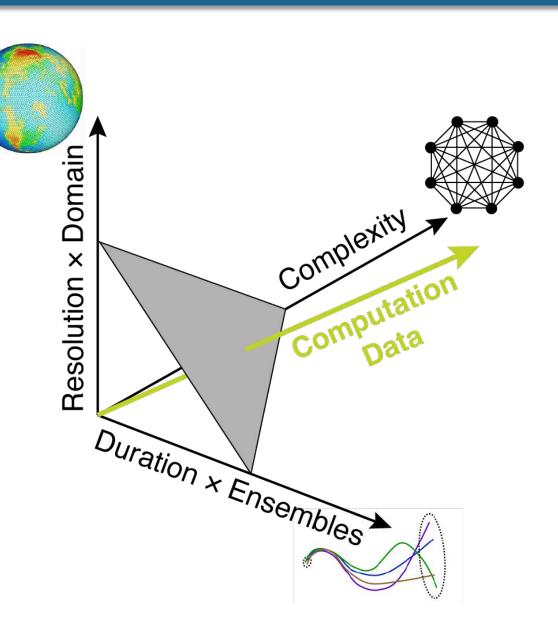
#### **Computational constraints**

Develop creative solutions

E.g., geophysical modeling + machine learning

Need hierarchy of modeling tools tailored to questions of interest

- Modeling systems built from interoperable components
- Enable bespoke sandboxes



### Interoperability between modular components

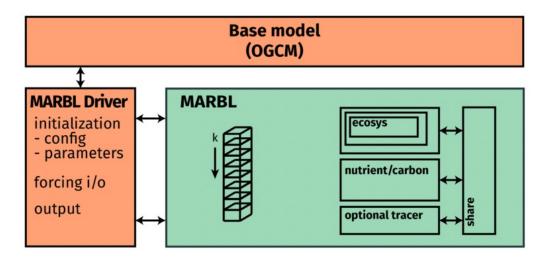
Modularity: facilitated by coupling infrastructure

Enable "mix-and-match" capabilities

Leverage interoperability to

- Isolate and study processes
- Explore structural uncertainty
- Leverage communities of practice

#### **Marine Biogeochemical Library (MARBL)**



$$\frac{\partial \varphi}{\partial t} + \nabla \cdot (\vec{u}\varphi) - \nabla \cdot (K\nabla\varphi) = \int J(\varphi)$$





#### **Computation and data constraints**

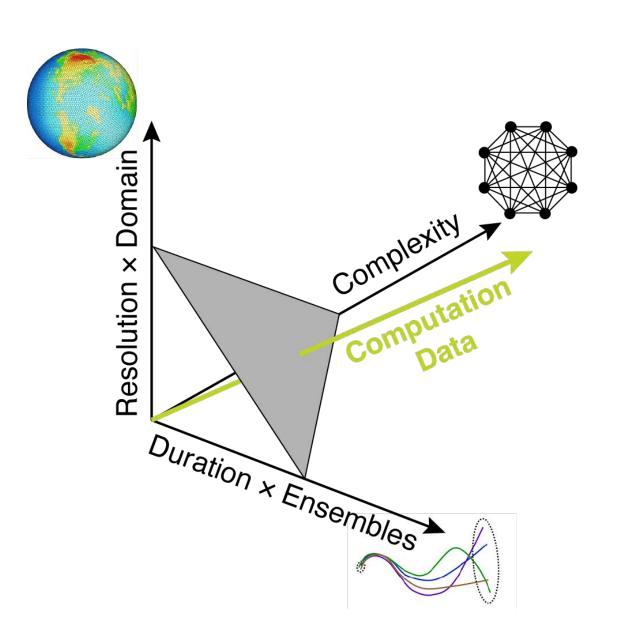
#### **Big Data**

Computation for *analysis* is a serious effort

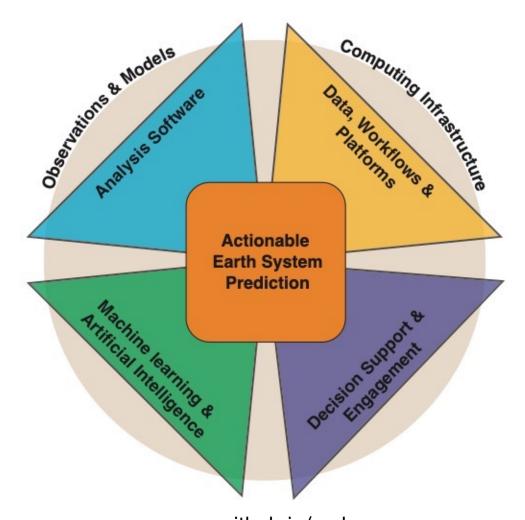
- Collaborative development
- Data science/ML

Decision support "dashboards"

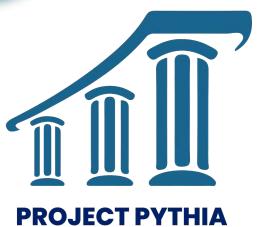
Computational Narratives: Platforms for community & policy engagement



### **Earth System Data Science**







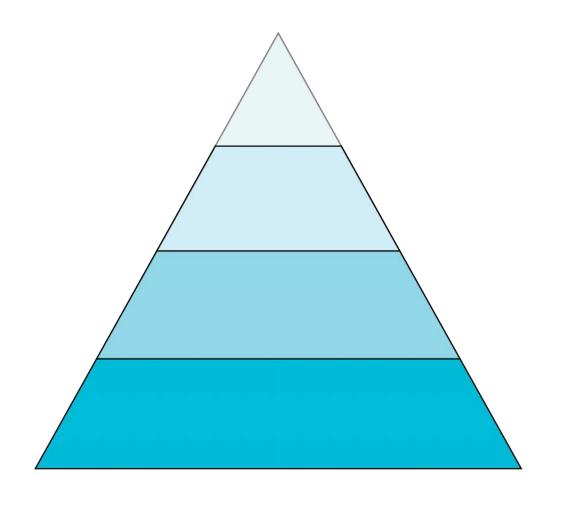
projectpythia.org







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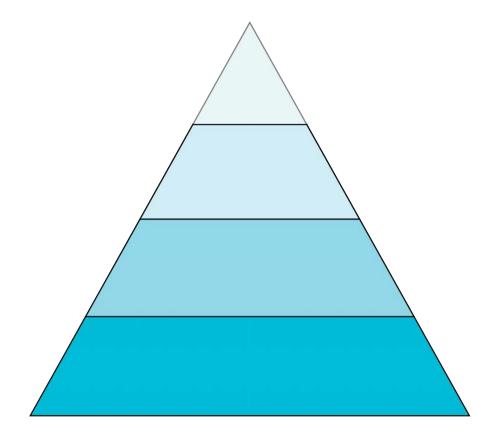
Data assimilation

Ocean physical and biogeochemical models

# **Proposal**

\$10M

Bespoke modeling applications



\$10M

Highly resolved observational deployments

